Metabolic cost of generating horizontal forces during human running

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Chang, Young-Hui, and Rodger Kram. Metabolic cost of generating horizontal forces during human running. J. Appl. Physiol. 86(5): 1657–1662, 1999.—Previous studies have suggested that generating vertical force on the ground to support body weight (BWT) is the major determinant of the metabolic cost of running. Because horizontal forces exerted on the ground are often an order of magnitude smaller than vertical forces, some have reasoned that they have negligible cost. Using applied horizontal forces (AHF; negative is impeding, positive is aiding) equal to −6, −3, 0, +3, +6, +9, +12, and +15% of BWT, we estimated the cost of generating horizontal forces while subjects were running at 3.3 m/s. We measured rates of oxygen consumption (VO2) for eight subjects. We then used a force-measuring treadmill to measure ground reaction forces from another eight subjects. With an AHF of −6% BWT, VO2 increased 30% compared with normal running, presumably because of the extra work involved. With an AHF of +15% BWT, the subjects exerted ~70% less propulsive impulse and exhibited a 33% reduction in VO2. Our data suggest that generating horizontal propulsive forces constitutes more than one-third of the total metabolic cost of normal running.

IN HUMANS AND OTHER LEGGED animals, the need to generate muscular force to support body weight (BWT) is a major determinant of the metabolic cost of steady-speed running. Taylor and colleagues (22) found a linear and proportional relationship between vertical loading with added mass and the rate of oxygen consumption (VO2) in humans and several other species. Additionally, Farley and McMahon (7) observed a proportional relationship between metabolic cost and the average vertical ground reaction force (GRF) using simulated reduced gravity to “unweight” human subjects. Kram and Taylor (12) showed that, in a variety of species across a wide range of speeds, the metabolic cost of running was proportional to the weight supported. These studies concluded that the vertical GRF (as opposed to the horizontal GRF) is a major determinant of the metabolic cost for steady-speed, level running. This seems reasonable because the peak vertical GRFs for running are an order of magnitude greater than peak horizontal GRFs (17), yet anyone who has run on a windy day intuitively knows that external horizontal forces can substantially affect the metabolic cost of running.

There have been only a few studies on the metabolic significance of horizontal force production during steady-speed running. Using a wind tunnel to apply horizontal impeding forces, Pugh (19) showed that the metabolic cost of treadmill running increased with the square of head-wind velocity, i.e., approximately proportional to the applied force. Others have found that metabolic cost increases proportionally with an increase in external work performed while the subject is running against an impeding force applied via a harness (4, 13, 23). We are aware of only one study that has investigated the metabolic effects of horizontal aiding forces. Davies (5) compared the metabolic cost of running with wind resistance vs. wind assistance for three subjects. He did not, however, directly measure forces applied to the runner, nor did he measure the forces exerted by the runner. Thus there is little biomechanical information available to explain the metabolic changes involved with horizontal loading.

Our aim was to alter the horizontal forces generated by the runner on the ground and to measure the corresponding changes in metabolic cost. We altered the horizontal forces generated by the runner by using an applied horizontal force (AHF). We compared the rates of VO2 and the integrated horizontal GRFs (impulses) for subjects running as we applied external horizontal aiding forces (+AHF) or external horizontal impeding forces (−AHF) at the waist. In doing so, we measured the changes in the propulsive and braking forces that subjects generated to compensate for the AHF. We then partitioned the relative importance of the horizontal propulsive forces vs. the horizontal braking forces generated during running. By measuring horizontal GRFs, we extended our understanding of running beyond previous studies of vertical and horizontal loading that did not measure the horizontal GRFs.

Our rationale for this study was that, when we provided an external horizontal forcing force, the reduction in VO2 would reflect the metabolic cost of generating the horizontal propulsive GRF during normal running. We anticipated that applying an impeding force would increase the VO2 and that an aiding force would decrease the VO2. Nevertheless, there is a strong correlation between vertical GRF and metabolic cost (7, 22), and our experiment did not alter these vertical forces. Thus our null hypothesis was that the absolute cost of generating horizontal forces on the ground would be relatively small and a minor determinant of the metabolic cost of running.

METHODS

Subjects. Experiments took place in two independent stages: metabolic measurements and biomechanical measurements.
Subjects gave informed consent before participating in the experiment, and the protocol was approved by the University of California Committee for the Protection of Human Subjects. For the metabolic experiments, we collected data on five men and three women ranging in age from 20 to 40 yr (27 ± 7 (SD) yr). Body mass ranged from 51.5 to 97.0 kg (68.6 ± 15.5 kg). For the biomechanics experiments, we collected data on four men and four women ranging in age from 20 to 36 yr (25 ± 5 yr). Body mass of these subjects ranged from 55.8 to 81.5 kg (65.8 ± 9.3 kg). All subjects were well-trained recreational runners. One year after collecting the VO2 data, we completed development of a force-treadmill capable of measuring vertical and horizontal GRFs (11). Because the subjects from the metabolic stage of the study were no longer available to participate in the biomechanical data collection, we recruited a new pool of subjects. The ideal experimental design would have been to collect both sets of data simultaneously from a single pool of subjects. Nevertheless, our specially designed force-measuring treadmill (11) had not been invented or built by the time the metabolic data were collected. It would have been possible to collect new metabolic data; however, we felt it was unnecessary, because all of the subjects showed the same pattern of response to the AHFs. Therefore, it is unlikely that either our results or our general conclusions would have changed substantially had we again collected the metabolic data.

Protocol. For the metabolic measurements, we habituated subjects to treadmill running within 7 days of actual data collection in accordance with procedures for kinematic accommodation to treadmill running (21). During the experimental sessions, subjects ran at a speed of 3.3 m/s on a motorized treadmill (Quinton 18–60) while we applied horizontal forces equal to −6, −3, +3, +6, +9, +12, and +15% of the subject's BWT. A negative value indicates an impeding AHF and a positive value indicates an aiding AHF. The order of applying aiding and impeding AHFs was randomized for each subject. Each data-acquisition trial lasted 8 min, and VO2 measurements were averaged for the last 4 min. Subjects rested 6 min between trials except when waiting for the treadmill belt direction to be reversed (which typically lasted 10–15 min). Subjects ran with zero AHF at both the start and end of the experiment. Although we did not measure maximal VO2 of the subjects, we determined that the subjects were exercising at a moderate-intensity level (18) because steady state was achieved within 3 min. Additionally, VO2 values for the zero AHF trials at the beginning and end of the experiment differed by <1%. For the biomechanical measurements, the protocol was similar to the metabolic experiment with the exception that trials lasted only a few minutes, and this second group of subjects ran on a specially designed force-measuring treadmill (11). Data were collected after allowing the subjects to run for 1 min at each condition. Morgan and colleagues (16) have previously shown that human running kinematic data are highly reliable and exhibit little variability over time.

Horizontal pulling apparatus. We applied aiding and impeding forces to the subjects via a waist belt worn near the center of mass (Fig. 1). The waist belt was connected in series with spring elements composed of rubber tubing that were stretched over a series of low-friction pulleys. The rubber tubing was stretched to two to three times its resting length so that small changes in length would not substantially change the applied force. Thus nearly constant horizontal forces were applied to the subjects. The magnitude of these AHFs was adjusted by altering the number of spring elements in parallel and by adjusting the length of the spring element with a hand wrench on the other end of the line.

We monitored the AHF with a force transducer in series with the line from the waist belt. Subjects were provided with a digital readout of the AHF and asked to maintain the appropriate level of force while running. AHFs were maintained within ±5% of the desired value across the entire range of applied-force conditions. Our method of applying horizontal forces differed from previous methods that used a rope connecting the subject to various weights hung over a low-friction pulley (4, 13, 23). The fore-aft oscillations of the center of mass while the subject is running on a treadmill could create substantial fluctuations in the AHF when an inertial mass is used to apply the force. Our design had a very-low-inertia compliant spring that resulted in a nearly constant AHF.

We calculated the average vertical GRF per step as well as the average peak vertical GRF per step for each subject to verify that only horizontal GRFs were altered by our apparatus. Across all conditions of AHF, neither the average vertical GRF nor the average peak vertical GRF changed significantly (P = 0.14 and 0.77, respectively). Thus we were confident that our apparatus applied external forces only in the horizontal direction. Furthermore, Davies (5) observed that, when subjects ran in a wind tunnel, they noticeably altered their posture by leaning into the wind. He noted that this leaning may have converted some potential drag forces into lift forces so that the external loads were no longer solely in the horizontal direction. Such a conversion of horizontal drag forces to vertical lift forces was not possible with our experimental apparatus.

Metabolic measurements. An open-flow system was used to measure the rate of VO2. Air was drawn from a loose-fitting mask to a variable-flow vacuum adjusted to draw air at a constant rate of 19.3 l/s. We determined that this was an adequate flow rate because an increase in the main flow of the system did not change the measured VO2. The expired air was sampled continuously and analyzed for oxygen content by using an electronic oxygen analyzer (Ametek S3A-II). The system was calibrated before each experiment by bleeding nitrogen into the mask at a known rate (0.2 l/s), and the rate of VO2 was calculated according to the nitrogen dilution technique (8). VO2 values were corrected to standard temperature and pressure. All data were recorded with a microcomputer by using virtual instrumentation software (LabView...
Variables showed significant trends (control value and average peak propulsive GRF was 43% of control value. Values represent means for 8 subjects).

In performing a study on the metabolic cost of generating horizontal forces, we recognize that there are many similarities between running on a level surface with an AHF and running on a hill. Despite some qualitative similarities between the two, there are some important quantitative differences between running on a hill and running on a level surface with an impeding or aiding force. An explanation of these quantitative differences is provided in the APPENDIX.

Statistical analysis. Metabolic and biomechanical data from this study were analyzed across all conditions of AHF by using a repeated measures design (ANOVA). We performed Tukey's honestly significant difference post hoc test to analyze the differences between each level of AHF. Significance was defined as P < 0.05.

Table 1. Metabolic and kinetic data for different applied horizontal-force conditions

<table>
<thead>
<tr>
<th>AHF (%body wt)</th>
<th>$\dot{V}_O_2$ (ml·kg$^{-1}$·min$^{-1}$)</th>
<th>Braking Impulse, N·s</th>
<th>Propulsive Impulse, N·s</th>
<th>Peak Braking Force, N</th>
<th>Peak Propulsive Force, N</th>
<th>Peak Vertical Force, N</th>
</tr>
</thead>
<tbody>
<tr>
<td>-6</td>
<td>45.7 ± 1.1</td>
<td>6.8 ± 0.5</td>
<td>20.8 ± 1.3</td>
<td>147.4 ± 6.0</td>
<td>238.0 ± 11.4</td>
<td>1,574 ± 91</td>
</tr>
<tr>
<td>-3</td>
<td>39.7 ± 0.9</td>
<td>10.1 ± 0.7</td>
<td>16.9 ± 1.1</td>
<td>189.3 ± 8.3</td>
<td>210.9 ± 10.9</td>
<td>1,583 ± 94</td>
</tr>
<tr>
<td>0</td>
<td>35.1 ± 1.0</td>
<td>13.9 ± 0.6</td>
<td>14.1 ± 0.6</td>
<td>227.2 ± 6.6</td>
<td>193.3 ± 7.0</td>
<td>1,670 ± 72</td>
</tr>
<tr>
<td>+3</td>
<td>30.4 ± 1.2</td>
<td>18.3 ± 1.2</td>
<td>11.7 ± 0.9</td>
<td>267.9 ± 15.7</td>
<td>172.3 ± 10.5</td>
<td>1,664 ± 126</td>
</tr>
<tr>
<td>+6</td>
<td>27.1 ± 1.2</td>
<td>22.9 ± 1.7</td>
<td>9.2 ± 0.7</td>
<td>293.8 ± 15.0</td>
<td>141.0 ± 9.5</td>
<td>1,633 ± 128</td>
</tr>
<tr>
<td>+9</td>
<td>25.2 ± 1.3</td>
<td>27.9 ± 2.0</td>
<td>7.5 ± 0.7</td>
<td>331.4 ± 15.5</td>
<td>123.1 ± 8.4</td>
<td>1,650 ± 137</td>
</tr>
<tr>
<td>+12</td>
<td>24.3 ± 1.4</td>
<td>33.2 ± 2.1</td>
<td>5.4 ± 0.6</td>
<td>387.5 ± 15.5</td>
<td>98.3 ± 8.5</td>
<td>1,699 ± 143</td>
</tr>
<tr>
<td>+15</td>
<td>23.7 ± 1.6</td>
<td>37.9 ± 2.5</td>
<td>4.2 ± 0.6</td>
<td>438.8 ± 20.5</td>
<td>83.3 ± 8.1</td>
<td>1,707 ± 114</td>
</tr>
</tbody>
</table>

Average active peak of vertical ground reaction force (GRF) did not change significantly across all horizontal loading conditions (P = 0.77). In contrast, at an impeding force of -6% body wt applied horizontal force (AHF), average peak braking GRF was 65% of zero AHF value and average peak propulsive GRF was 123% of control value. At an aiding force of +15% body wt AHF, average peak braking GRF was 193% of control value and average peak propulsive GRF was 43% of control value. Values represent means for 8 subjects ± SE of the mean. All variables showed significant trends (P < 0.01) except for mean active peak of vertical GRF.
shown in Fig. 3. The average horizontal impulses exerted per step for each condition are shown in Fig. 4. With an impeding force (−AHF), the horizontal braking impulse decreased, whereas the horizontal propulsive impulse increased. Conversely, the horizontal braking impulse increased, whereas the horizontal propulsive impulse decreased with aiding force (+AHF). As indicated in Fig. 3, the vertical GRF impact peak was altered appreciably with the level of AHF, but the active peak did not change. The impact (or passive) peak of the vertical GRF is thought to be caused by the collision of the heel (or the “effective mass” of the shank) with the ground (6). Despite these changes in the impact peak of the vertical GRF, the average vertical force per step for every trial was never >1.6% different from the control condition. A summary of the kinetic data is provided in Table 1.

The typical horizontal GRF pattern for a person running at a steady speed on level ground consists of an initial braking phase (observed as a negative reaction force that decelerates the forward movement of the person) that is followed by a propulsive phase (observed as a positive reaction force that accelerates the person in the direction of travel; Ref. 17). Note that, in the zero AHF case (Fig. 3A), the horizontal braking and propulsive impulses were equal and opposite as is necessary for steady-speed running on a level surface. Of course, this relationship did not hold when an AHF was used (Fig. 3B and C), because the horizontal braking and propulsive impulses generated by the runner were altered to compensate for the external AHF to maintain a steady speed.

The stride kinematics of running were largely unaffected across all AHF conditions. The average stride frequency did not change significantly (P = 0.15) across all conditions. The average time of ground contact did change significantly (P = 0.03) but never more than ±0.01 s compared with the control condition. A summary of the kinematic data is provided in Table 2.

**DISCUSSION**

At the greatest level of horizontal aiding force (+15% BWt AHF), the metabolic rate of our subjects decreased by 33% from the metabolic rate of normal running. At this +15% BWt AHF condition, the runners were

<table>
<thead>
<tr>
<th>AHF, % body wt</th>
<th>Stride Frequency, Hz</th>
<th>Time of Contact per Step, s</th>
<th>Duty Factor</th>
</tr>
</thead>
<tbody>
<tr>
<td>−6</td>
<td>1.46 ± 0.03</td>
<td>0.268 ± 0.009</td>
<td>0.39 ± 0.01</td>
</tr>
<tr>
<td>−3</td>
<td>1.45 ± 0.03</td>
<td>0.269 ± 0.007</td>
<td>0.39 ± 0.01</td>
</tr>
<tr>
<td>0</td>
<td>1.40 ± 0.02</td>
<td>0.263 ± 0.003</td>
<td>0.37 ± 0.01</td>
</tr>
<tr>
<td>+3</td>
<td>1.41 ± 0.03</td>
<td>0.258 ± 0.006</td>
<td>0.37 ± 0.01</td>
</tr>
<tr>
<td>+6</td>
<td>1.41 ± 0.03</td>
<td>0.260 ± 0.005</td>
<td>0.37 ± 0.01</td>
</tr>
<tr>
<td>+9</td>
<td>1.39 ± 0.03</td>
<td>0.261 ± 0.007</td>
<td>0.36 ± 0.01</td>
</tr>
<tr>
<td>+12</td>
<td>1.40 ± 0.03</td>
<td>0.253 ± 0.006</td>
<td>0.35 ± 0.01</td>
</tr>
<tr>
<td>+15</td>
<td>1.43 ± 0.02</td>
<td>0.253 ± 0.006</td>
<td>0.36 ± 0.01</td>
</tr>
</tbody>
</table>

There were no substantial changes in kinematic variables measured at each horizontal loading condition. Average stride frequency did not change significantly (P = 0.15) across all conditions. Both average time of contact and average duty factor (fraction of stride period that 1 foot spends in contact with ground) showed slight but significant trends (P = 0.03). Values represent means for 8 subjects ± SE of the mean.

Fig. 3. Typical vertical (Fv) and horizontal (Fh) ground reaction forces for 3 steps of 1 subject: for unloaded, 0% body wt AHF control condition (A), with an impeding force of 6% body wt AHF (B), and with an aiding force of 15% body wt AHF (C).

Fig. 4. Braking impulses and propulsive impulses vs. AHF (in %body wt). All values are normalized to unloaded, control condition (%body wt AHF). Values are means for 8 subjects. Error bars represent SE of mean.

Table 2. Kinematic data for different applied horizontal-force conditions

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**Fig. 3.** Typical vertical (Fv) and horizontal (Fh) ground reaction forces for 3 steps of 1 subject: for unloaded, 0% body wt AHF control condition (A), with an impeding force of 6% body wt AHF (B), and with an aiding force of 15% body wt AHF (C).
applying 70% less propulsive impulse per step compared with what they applied without any AHF. This suggests that the metabolic cost of generating horizontal propulsive forces during normal running constitutes more than one-third of the total cost of steady-speed running. For this reason, we reject the hypothesis that the generation of horizontal forces during normal running has negligible cost.

This decrease in metabolic rate with horizontal aiding forces occurred despite a dramatic increase in braking forces. For the +15% BWt AHF condition, braking impulse increased by 172.7%, yet we measured a net decrease in metabolic rate. Furthermore, with a horizontal impeding force of −6% BWt, the metabolic rate increased by 30.2%, despite a 51.1% decrease in braking impulse. At this condition, propulsive impulse increased 47.5%. Therefore, it is plain to see that the generation of horizontal propulsive forces is metabolically much more expensive per unit of force than the generation of horizontal braking forces during steady-speed running.

Generating horizontal forces was more expensive per unit of force than was generating vertical forces. For a +15% BWt AHF, the average decrease in propulsive force generated per step was 57.5 N. Expressed per unit of body mass, the corresponding decrease in VO$_2$ was 11.4 ml·kg$^{-1}$·min$^{-1}$. This decrease in the rate of VO$_2$ is equivalent to 262.0 W. Thus this suggests that generating 1 N of horizontal propulsive force on the ground during steady-speed running at 3.3 m/s normally costs at least 4.6 W. Farley and McMahon (7) saw that, for a 25% decrease in average vertical force, there was a concomitant 25% decrease in VO$_2$. Assuming a similar relationship for our data, we see that generating 1 N of vertical force on the ground during steady speed at 3.3 m/s would cost 1.2 W. Thus per unit of force generated, horizontal propulsive forces are almost four times more expensive than vertical forces. These results probably reflect the relative lengths of the moment arms over which these forces are applied. When moments (or torques) about each leg joint are considered, a unit of force generated horizontally on the ground would have a much greater effect than a unit of force generated vertically (especially at the more proximal joints).

At first glance, our findings seem to disagree with the data of Farley and McMahon (7) and Taylor and colleagues (22), who suggested a one-to-one relationship between metabolic cost and the generation of vertical forces. Their interpretation left little room for horizontal forces to play a role in determining the metabolic cost of running. Perhaps it is a naive notion to simply consider vertical and horizontal forces as separate determinants of the metabolic cost of running. It is the net resultant force generated on the ground that affects the net muscle moment at each joint as well as the force of each muscle crossing the joint. In reconciling this difference, we suggest that it may not be appropriate to consider vertical and horizontal GRFs as independent determinants of metabolic cost as they are conceptual rather than physiological constructs.

Future research investigating the influence of external perturbations on the metabolic cost of running should consider the effects of the resultant vector of the vertical and horizontal forces applied to the ground during level running.

**APPENDIX**

Qualitatively, both running against a horizontal impeding force and running uphill require more external work and, therefore, more power output by the runner. Similarly, a horizontal aiding force and downhill running require less external work and less power output by the runner. Both running with an AHF and running on a hill result in similar qualitative changes in metabolic cost. Nevertheless, there are critical differences between the two running conditions that reveal that they are not quantitatively the same.

One difference is in the efficiencies for each running condition. When running up a hill of some angle ($\phi$), gravity exerts an impeding force equal to mg sin($\phi$), where mg = BWt. It is important to note that this calculation of the impeding force is performed with respect to the reference frame of the hill such that the angle of the hill defines the horizontal plane. With this equation, an “equivalent” hill angle ($\phi_e$) can be found where an impeding force equivalent to the AHF from our study can be calculated. In this way, we can calculate the work efficiencies as defined by Gaesser and Brooks (9) and compare them with similar values found in the literature for running both with impeding forces and along equivalent hill angles. Work efficiency is calculated as the external work rate divided by the corresponding increase in metabolic rate at zero load (i.e., zero load = normal level running).

Our measurements of work efficiency are substantially higher than what has been reported for uphill running. At the −3% BWt AHF, our data indicated a work efficiency of 62.6%. Pugh (19) measured a similar work efficiency of 69.0% for running into a head wind at a similar mechanical power output, whereas he measured a work efficiency of 45.6% for running up an equivalent hill angle (i.e., at the same mechanical power output). At the −6% BWt AHF, our data showed a work efficiency of 54.5%. We calculated a substantially lower work efficiency of 46.6% for running up a hill angle equivalent to our −6% BWt AHF by using the relationships reported by Bassett and colleagues (1). These data suggest that running on level ground with an AHF is quantitatively different from running up a hill.

Some studies have suggested that the efficiencies for running with a horizontal force were the same as the efficiencies for uphill running (5, 13, 23). These studies were difficult to compare and evaluate, however, because efficiency values were either averaged for a wide range of power outputs or else $\Delta$efficiencies were given for comparison rather than work efficiencies ($\Delta$efficiency is defined as the change in work rate divided by the change in metabolic cost; Ref. 9).

A second difference between running with an AHF and uphill running is that the stride frequency does not change with the amount of AHF, whereas stride frequency increases considerably with increasing hill angles (14, 15). This suggests that the internal work (to swing the legs relative to the center of mass) for running with an AHF does not change with horizontal force, whereas internal work does increase with uphill running (14). This increase in internal work with hill angle may be one reason that work efficiency is lower for uphill running compared with running with an AHF.

A third important difference between running with an AHF and running up a hill is the posture that the runner adopts. In
both cases, runners tend to align their trunks relative to the gravitational vector rather than relative to the ground. The runners in our study maintained an upright posture when running with a horizontal force, whereas Iversen and McMahon (10) quantified how runners leaned forward relative to the reference frame of the hill angle.

Differences in posture probably change the orientation of the GRF vector relative to the leg joints. This would alter the effective mechanical advantage and thus the operation of the muscles and tendons during running (2). Indeed, the differences in the efficiencies and stride kinematics for running with an AHF vs. running up a hill indicate that the muscles and tendons function differently in each condition. Normal running is a bouncing gait and involves the storage of both gravitational potential energy and horizontal kinetic energy as elastic energy. Running on the level with an AHF does not affect the change in gravitational potential energy, whereas running up a hill clearly does. The springlike mechanics of normal running are crucial for conserving metabolic energy. Roberts and colleagues (20) showed that turkeys utilize less elastic energy storage when running uphill than when running on level ground. The high efficiencies we observed in the efficiencies and stride kinematics for running with an AHF vs. running up a hill indicate that the muscles and tendons are storing more elastic energy compared with humans running up a hill. For these reasons, running up a hill is quantitatively different from running with an AHF.

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