Breath-by-breath analysis of cardiorespiratory interaction for quantifying developmental maturity in premature infants

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A CURRENT CONCEPT OF HEALTH is that organs couple with one another through extracellular signaling or the nervous system. Illnesses such as systemic inflammation disrupt this complex, finely adaptive system and lead to uncoupling (17). When the organs have obvious oscillatory dynamics as the heart and the lungs do, presence of coupling is taken as a sign of good health. The cardiorespiratory interaction is mediated through complex central and autonomic nervous system mechanisms. Consipicuous examples of such interaction are respiratory sinus arrhythmia and cardioventilatory coupling. Respiratory sinus arrhythmia (RSA) is the familiar rise and fall of heart rate with respiration (10, 18, 27, 42), mediated by the baroreflex, respiratory gating, or both (9, 11, 26). Presence of RSA correlates with good outcome in a number of clinical situations, including intensive care (1, 37, 39). Cardioventilatory coupling (CVC) is the preferential synchronization of inhalation at integer ratios with the heartbeat, mediated by baroreceptor inputs to the respiratory pattern generator (52). The presence of CVC has been documented in neurologically healthy adults in sleeping states and under anesthesia (16, 33, 51).

Coupling of heart rate and ventilation is present in healthy infants born at term (23), infants born preterm (3, 25), and even in late-term fetuses (19). Respiratory control of cardiac dynamics has been shown to increase with postnatal age in anesthetized term piglets (24). Here, we study continuous changes in cardiorespiratory interaction in waking term and preterm infants. Late gestation is a busy time with regard to development of central nervous system interconnections that reside between and within the brain stem and limbic system and underlie cardiorespiratory interaction (6). The complex integration of signaling processes and receptor expression proceeds in a presumably orderly but, to the outside observer, highly nonlinear way, especially when major portions of the development take place postnatally in the premature infant in the Neonatal Intensive Care Unit (NICU). These concepts are of clinical relevance in bedside neonatology. Determining an acceptable level of physiological maturity is an important task assigned to the clinician caring for the NICU patient who was born preterm. For example, nearly all infants born very preterm (<1,500 g birth weight) will have at least one life-threatening apneic event during their initial hospitalization. Clinicians caring for such babies are challenged with deciding when the infant has sufficient physiological maturity to be discharged safely into an environment lacking the intensive and continuous cardiorespiratory monitoring available in the NICU setting (7). Mature physiological cardiorespiratory interaction might not be just a matter of waiting until a consensus postmenstrual age, since fully functional physiological maturity of respiratory control comes later and later the more prematurely an infant is born (7, 13). The presence of apparent life-threatening apneic events (5) and SIDS (28) in the first several months after birth in premature infants suggests that, for some, physiological maturity comes late if at all.

Although the degree of cardiorespiratory interaction might provide information about the maturation process, it is hard to
measure. Variations in breathing frequency and depth, and in the lag between ventilation and heart rate can confound temporal and frequency domain analysis of cardiorespiratory interaction in infants (21–23). Confident detection of cardiorespiratory interaction requires high-quality EKG and chest impedance signals. The long, uninterrupted time series data required to achieve this using conventional time- and frequency-domain analysis are not common enough to permit study of cardiorespiratory interaction in the NICU. Another approach is to use techniques that are insensitive to missing data. One such approach is to identify individual beats and breaths only when the data allow, and Schäfer and coworkers gave an example of this approach in a study of cardiorespiratory interaction in young adults (46). In the present work, we followed their technique for determining the probability of heartbeats as a function of respiratory phase as a measure of cardiorespiratory interaction. The fundamental assumption is that differential distribution of heartbeats within the respiratory cycle is evidence for cardiorespiratory interaction.

Cardiorespiratory interaction, even when measured well, is only intermittent at best. In eight young adults carefully studied at rest, Schäfer and coworkers found evidence for coupling for only ~30 min of the 4 h studied. In infants, it is, for example, more prevalent during quiet sleep than REM sleep (20, 21). Our major hypothesis is that measuring cardiorespiratory interaction in premature infants may be clinically useful in assessing the developmental maturity of physiological coupling. To begin to test this idea, we have measured cardiorespiratory interaction in a large population of consecutively admitted infants in a tertiary care NICU. To this end, we implemented phase-based measures (46) in an effort to quantify the effect of breathing on the heartbeat, the predominant direction for cardiorespiratory interaction in infants (38). We present our methods for automatically analyzing continuous physiological waveforms and the relation between this measure of coupling and developmental maturity, and discussion of the underlying mechanisms.

METHODS

Ethical approval. The University of Virginia (UVA) Institutional Review Board gave permission for this study. This is an observational study, and no experiments were conducted on humans.

Patient population. We collected cardiorespiratory waveforms continuously from the bedside monitors of 1,202 infants admitted consecutively to the UVA NICU from January, 2009 through June, 2011. Patient demographic data, including admission and discharge dates, types and times of respiratory support, and disposition and status at discharge were obtained from the clinical records of 292 very low birth weight (VLBW: <1,500 g at birth) infants.

Table 1. Demographic information for infants in the University of Virginia Neonatal Intensive Care Unit from January 2009 to June 2011

<table>
<thead>
<tr>
<th>Population</th>
<th>N</th>
<th>Birth Weight, g</th>
<th>Gestational Age, wk</th>
<th>Males</th>
</tr>
</thead>
<tbody>
<tr>
<td>All</td>
<td>1,202</td>
<td>2,339 (1,615)</td>
<td>35 (7)</td>
<td>644</td>
</tr>
<tr>
<td>Non-VLBW</td>
<td>910</td>
<td>2,705 (1,120)</td>
<td>37 (5)</td>
<td>493</td>
</tr>
<tr>
<td>VLBW</td>
<td>292</td>
<td>1,010 (500)</td>
<td>27 (4)</td>
<td>151</td>
</tr>
<tr>
<td>Discharge home (VLBW)</td>
<td>148</td>
<td>1,140 (494)</td>
<td>28.5 (4.5)</td>
<td>79</td>
</tr>
</tbody>
</table>

VLBW, very low birth weight. *Birth weight and gestational age values are medians (interquartile ranges).

Of these, 148 were discharged to home without any respiratory support, including supplemental oxygen. These infants were therefore considered to have recovered from all acute illnesses encountered during the study period and had been judged by the attending physician to have adequate cardiorespiratory stability to be discharged from the hospital without cardiorespiratory monitoring. Analysis of waveforms from VLBW patients was restricted to times without endotracheal intubation, since mechanical ventilation may alter the relationship between respiratory and cardiac control. Estimated gestational age (EGA) was calculated as the time from the date of onset of the mother’s last menses to the date of birth. Post menstrual age (PMA) was calculated as the time from the date of onset of the mother’s last menses to the time of analysis, regardless of the date of birth. Table 1 shows demographic information for the study population. Figure 1 shows a schematic of the UVA NICU dataset. This real-world clinical dataset was limited by absence and poor quality of chest impedance. Nonetheless, 3.3 patient-years of cardiorespiratory interaction were found. Results are shown for non-VLBW infants, extubated VLBW infants, and intubated VLBW infants.

Data acquisition. We monitored infants in the NICU with GE bedside monitors using three electrocardiogram (EKG) leads digitized at 240 Hz. A small-amplitude and high-frequency voltage is applied between two of the EKG leads. The chest impedance pneumograph is the applied voltage divided by the measured current, and was digitized at 60 Hz. A central network server (BedMasterEx, Excel Medical, Jupiter, FL) behind a clinical firewall collected these data and transmitted them to a customized parallel storage and computing cluster behind an additional firewall. Data were analyzed in parallel on a 10-computer cluster with 80 processors, 40 GB of RAM, and 100 TB of hard disk space. A total of 60.7 patient-years of data (4 TB) were collected from bedside monitors of 1,202 infants in the University of Virginia NICU. Waveforms were analyzed in three steps: noise quantification, breath and QRS detection, and measurement of cardiorespiratory interaction.

Waveform analysis: noise quantification. Our measurement of cardiorespiratory interaction relies on automated detection algorithms that require minimal noise. We quantified noise levels by adding noise of clinically appropriate frequency content to noise-free waveforms and calculating signal quality indexes. Clinically appropriate noise was derived from an analysis of a large sample of clinical data from many infants. Signal quality indexes were analyzed as a function of added noise, and we restricted further analysis to signals with low estimated noise levels. Detailed discussion of signal quality measures for EKG and chest impedance time series are provided in the APPENDIX.
Waveform analysis: breath and QRS detection. QRS complexes were automatically identified on the EKG lead with the lowest noise using three detection algorithms. One is threshold-based (40) as implemented by Clifford and coworkers (35, 50). The second removes the T- and P-waves by using a high-pass filter. QRS complex locations were defined as positive crossings of the x-axis in Hilbert space (30). The final method decomposed the EKG signal using a continuous Haar wavelet transform at scales 2^n, where n = 1, 2 ... 5. The squared normalized wavelet coefficients were averaged, the root-mean-square over 80 ms was calculated, and 80-ms segments were centered at peaks in the resulting signal collected. Segments that had significant correlation (P < 0.01) with at least 50% of other segments were defined as QRS complexes. Complexes detected by each method were represented with kernels of unit height and width of 80 ms at three standard deviations. The three kernelled time series were averaged, such that peaks identified by all three methods within the same 80-ms window had minimum amplitude of 0.67. We defined heartbeats as peaks exceeding the value 0.8 in the averaged signal based on visual inspection. The root mean squared difference between averaged heart rate from the monitor and our detection scheme was 1.8 beats/min.

Features of interest in the chest impedance pneumograph are times at which the lungs are full and empty. Cardiac artifact was removed from the signal using a heart time transform (34). Full and empty lung states were found using peak and trough detection on a zero-phase band-pass filtered signal. A high-frequency cutoff was defined using a discrete Haar wavelet transform of the chest impedance time series normalized to mean 0 and variance 1. The variance was calculated at each scale, and the respiratory band was identified by collecting scales with the most variance until at least 87%, or (1 - e^{-2}), of the total variance was included. The high-frequency cutoff was defined by the largest scale below the respiratory band. The low-frequency cutoff was varied using MatLab (MathWorks, http://www.mathworks.com) implementations of golden section search and parabolic interpolation. The minimization criterion was the coefficient of variation for the Hilbert space amplitude. The minimization was bounded by frequencies corresponding to the length of the time series and the shortest scale above the respiratory band.

Waveform analysis: measurement of cardiorespiratory interaction. To quantify cardiac dependence on respiration, we studied the temporal association of heartbeats within the respiratory phase. Each heartbeat was assigned a value corresponding to the phase of respiration at which it occurred. The probability of a heartbeat was calculated as a function of concurrent respiratory phase using a kernel density estimate. Interaction of heart to lungs led to localization of heartbeats within the respiratory cycle that was evident in the probability densities. We created these probability density functions every 30 s for sliding windows of 4 min. We used the Shannon entropy (48), S, of the probability density function to quantify the degree of localization of heartbeats in respiratory phase. Lower values of entropy denote more localization of heartbeats in a respiratory phase and, therefore, more coupling.

We define a measure of cardiorespiratory interaction, C, as the fraction of overlapping 4-min records in a 2-h period that had a <0.1% probability of arising from noise. The minimum number of 4-min windows was 10, with at least 30 heartbeats each. This corresponds to a minimum of 11–40 min every 2 h.

RESULTS

Selection of data for analysis. Although 61 patient-years of data were collected, not all data were suitable for the analysis of cardiorespiratory interaction. Although the noise in the EKG signal was generally low enough for QRS detection, the chest impedance signal was of more variable quality. High-quality EKG data (<20% noise) were available in 99% of the dataset. Only 55 patient-years of the dataset had chest impedance recorded. We accepted chest impedance signals having noise commensurate with a sine wave plus 85% additional noise. We found that 33% of available data, corresponding to 18 patient-years, were of sufficiently low noise for analysis. We justified the inclusion of data with such a large apparent noise component because both normal respiratory variability and normal non-sinusoidal breathing are detected as noise in our analysis. The chest impedance in Fig. 2A, for example, has an estimated noise of 21%.

An example of the analysis. Figure 2, A and B, shows two exemplary time series of EKG and chest impedance from the same infant. In Fig. 2A, alternating QRS complexes repeatedly occurred in mid-exhale and mid-inhale. In Fig. 2B, the timing of QRS complexes varied throughout the time series. The probability densities for heartbeats as a function of respiratory phase for 4-min records containing these time series are shown in Fig. 2C, showing that the timing of heartbeats depended on the respiratory state in Fig. 2A but not in Fig. 2B. It is important to note that these two windows have comparable heart rate variability: 94.7 and 95.4 beats/min², respectively. This indi-
cates that this measure of heartbeat synchronization to respiration is distinct from conventional heart rate variability metrics.

The probability density represented by the solid line in Fig. 2C showed dependence of heartbeat timing on respiration, whereas the probability density represented by the broken line did not. We quantified the difference using the Shannon entropy. The probability densities shown as solid and broken lines in Fig. 2C have Shannon entropies of $S = 1.611$ and $S = 1.787$, respectively, where the maximum possible entropy is $\ln(2)$, or 1.84.

Availability of data for analysis. Figure 3A shows the histogram of number of days that met our criteria for signal quality and were analyzed for cardiorespiratory interaction in 1,202 patients. The mean number of records per patient was 34,600, corresponding to an average of 13 days of data per patient. Figure 3B shows the histogram of proportion of each patient’s stay that met our criteria for signal quality and was analyzed for cardiorespiratory interaction. On average, we analyzed cardiorespiratory interaction in 52% of each patient’s stay.

Non-randomness of the probability densities. Figure 4A shows the histogram of Shannon entropy of the probability densities (for example, shown in Fig. 2C) resulting from a series of random numbers in 1.7 million trials. We expect a uniform distribution of heartbeats in respiratory phase to simulate uncoupled cardiorespiratory dynamics. The entropies are shown as a function of the number of heartbeats in the trials. The 0.1% value for each heartbeat count is shown as a solid line. Thus, at each heartbeat count, 99.9% of entropy values from random trials were above this curve.

Figure 4B shows the histogram of actual entropy and heartbeat count values for 1.7 million 4-min records from the NICU dataset. The circles represent the examples given in Fig. 2, A and B. Since points under the solid line have only 0.1% chance of occurring from a random process, we classified them as coupling of heartbeats and breaths. We find that 25.7% of measurements show coupling, i.e., have a <0.1% chance of arising from random numbers.

Mechanism of cardiorespiratory interaction. We calculated cardioventilatory coupling in each record using the methods of Tzeng et al. (52) to investigate the relation to our measure of cardiorespiratory interaction. We calculated the Shannon entropy of histograms of the time between inhale and the previous R-wave, and classified records whose entropy had a <5% chance of occurring from noise given the number of intervals as exhibiting cardioventilatory coupling (52). We found only moderate agreement between the two measures (Cohen’s kappa statistic $\kappa = 0.33$).

To investigate the relationship between RSA and cardiorespiratory interaction, we investigated the preference for heartbeats during inhale or exhale. Figure 5 shows the probability density for the fraction of heartbeats during inhale for all records from VLBW infants at times with no respiratory support and where cardiorespiratory interaction was evident. The fraction of heartbeats during inhale was determined by integrating the right half of the probability density of heartbeats as a function of respiratory phase. This process shifts the mode...
of the distribution in Fig. 5 toward fewer beats during inhale due to stretching of exhale. The distribution in Fig. 5 is bimodal with a second peak in the distribution at 0.43; this indicates preferential beating of the heart during exhale. Respiratory sinus arrhythmia, on the contrary, induces a high heart rate during inhale and should elicit preferential beating of the heart during inhale.

The degree of cardiorespiratory interaction was a function of PMA, but not of birth weight or gestational age at birth. Figure 6 shows cardiorespiratory interaction as a function of postmenstrual age (PMA), the sum of EGA at birth and time since birth. Non-VLBW infants were included in the analysis regardless of their ventilatory status. VLBW infants were included in the analysis only when they were extubated.

Figure 6A shows the distribution of patients analyzed: non-VLBW infants (filled bars), extubated VLBW infants (open bars), and their union.

Figure 6B shows cardiorespiratory interaction as a function of PMA for non-VLBW infants (black lines) and extubated VLBW infants (gray lines). Solid lines represent the mean, and broken lines represent the 95% confidence interval. Cardiorespiratory interaction increased with PMA in both populations. There was, in fact, no statistically significant difference in cardiorespiratory interaction between non-VLBW patients and extubated VLBW patients after 32 wk PMA as tested by signed rank tests.

Figure 6C shows cardiorespiratory interaction as a function of PMA for infants with estimated gestational ages (EGA) of <32 wk at birth (gray lines) and EGA of ≥32 wk at birth (black lines). Cardiorespiratory interaction increased postnatally in both groups. In fact, between 32 and 38 wk PMA, cardiorespiratory interaction for the two groups was essentially identical. The falling number of VLBW infants after 38 wk made comparison more difficult. This analysis was based on EGA at birth and PMA, and did not consider birth weight or respiratory support. Thus each group has extubated VLBW infants and non-VLBW infants whose respiratory support was not known.

Clinical utility: safe discharge from the NICU. Figure 7 shows cardiorespiratory interaction as a function of time relative to discharge home without respiratory support for 148 extubated VLBW infants. The median prevalence of cardiorespiratory interaction in the previous 72 h was calculated for each infant each hour. Values are mean cardiorespiratory interaction for all infants each hour. The shaded region is the 95% confidence interval around the mean. The prevalence of cardiorespiratory interaction increased over the 7 wk before discharge. A signed rank test between values 30 days and 10 days before safe discharge home (broken lines) indicates the medians at these points were significantly different ($P < 0.001$).

DISCUSSION

We studied cardiorespiratory interaction in 1,202 NICU infants using a breath-by-breath measure of cardiorespiratory interaction originally presented by Schäfer and coworkers (46).
Our major finding was that cardiorespiratory interaction increased with postnatal age, as measured from 26 wk to approximately full-term gestation. Surprisingly, this relationship was independent of both the birth weight and the gestational age at birth. This indicates that development of cardiorespiratory interaction through the central and autonomic nervous systems may be insensitive to environmental influences. We also find that prevalence of interaction steadily increased during the 7 wk before the attending physician’s decision to discharge the baby to home without respiratory support or cardiorespiratory monitoring.

The strength of our analytical approach was that each breath and heartbeat was identified individually in determining the respiratory phase at which each heartbeat fell. This eliminated respiratory and heart rate variability as confounders. Additionally, R-R intervals were not required by this measure, making it robust to missing beats, and the phase-based measure is not subject to cardiac aliasing, a common issue in frequency domain analysis of neonatal heart rate (45, 53). Finally, all signals were collected from conventional bedside monitors that are routinely operational throughout the hospitalization of all high-risk neonates, without the requirement of additional interfaces or technical attendance.

One limitation is that we did not collect respiratory support information for non-VLBW infants. For VLBW infants, we excluded times of mechanical ventilation since our ultimate goal was to find a reliable indicator of cardiorespiratory stability that could be used to help the clinician decide on the timing of a safe apnea-free discharge of the spontaneously breathing baby born prematurely. Another limitation is the requirement for very high-quality bedside monitoring (4). The usual reason for exclusion was noise in the chest impedance signal. We acquired 61 infant-years of data and found 18 yr that had suitable chest impedance for reliable breath detection. We found 3.3 yr of cardiorespiratory interaction, ~18% of the analyzed time.

This is comparable with the original finding by Schäfer et al. of ~30 min of cardiorespiratory interaction in 4 h of recording (46). Other signals such as air flow measured by nasal thermistor or strain-gauge-based chest belts might increase proportionally where accurate cardiorespiratory interaction might be measured, although long periods of recording many babies under such conditions would be impractical in the usual NICU environment. Finally, we note that one possible explanation of our results is that cardiorespiratory interaction is a surrogate for quiet sleep (16, 20, 21). This is particularly relevant in the context of CVC, which is only observed in resting or sedated subjects (16, 51). A rigorous comparison with continuous sleep measures would be necessary to quantify this relationship.

We quantified cardiorespiratory interaction by the temporal association of heartbeats within the respiratory cycle. The measurement does not allow distinction, though, between the scenarios in which breathing dictates the timing of heartbeats (RSA) or the opposite scenario in which heartbeats dictate the timing of breaths (CVC). Schäfer et al. find that the prevalence of cardiorespiratory synchronization is diminished in patients with significant RSA (46), and Galletly and Larsen find this to be the case with CVC as well (15). Coupling in this context is mediated by baroreceptor inputs to the central respiratory pattern generator (52) and is only found in patients under anesthesia or in resting states (16, 51). We find only moderate agreement between the temporal association of heartbeats within the respiratory cycle and CVC. We also find no direct evidence for RSA in our dataset of neonatal intensive care patients. These findings indicate that multiple mechanisms contribute to our measure of cardiorespiratory interaction, and those mechanisms are uncertain. Future studies should be designed to investigate the underlying physiology of cardiorespiratory interaction by analyzing, e.g., variations in the probability density of heartbeats as a function of respiratory phase with PMA.

Regardless of the underlying coupling mechanisms, our findings demonstrate that cardiorespiratory interaction coincides with development of brain stem maturity in preterm infants. The prevalence of apnea of prematurity in neonatal intensive care patients declines with increasing PMA (6). This indicates improving central respiratory control in the ventrolateral medulla. A subset of cardiac motoneurons cohabit this region and develop interconnectivity with the neurons in the ventral respiratory column (49). Neural connections between these groups result in dependence of inter-heartbeat intervals on phase of respiration at which the beat occurred (12). Therefore, development of cardiorespiratory interaction should reflect brain stem development, whether mediated by baroreceptor afferents or sleep architecture in the case of CVC (16, 52), or by chemosensory pathways, the baroreflex loop, or respiratory gating in the case of RSA (8, 9, 11, 26, 27).

Future studies will be required to understand the link of coupling to other measures of brain stem maturity, such as independent thermoregulation, coordination of sucking and breathing, and decreasing incidence of apnea. Moreover, we hypothesize that providing measures of cardiorespiratory interaction to critical care professionals will lead to safer and earlier discharge of prematurely born infants from intensive care. Continuous monitoring of premature infants using advanced mathematical approaches (2, 14, 29, 31) can also improve outcomes by identifying impending illness early, thus affording the clinician the ability to intervene sooner. This capability has been demonstrated in the large randomized trial of heart rate characteristics monitoring for early detection of neonatal sepsis (36). Since coupling of organs is correlated
Signal quality measures were then calculated at each value of appropriate noise time series with unit variance, and fraction of variance due to noise. The time series from the time series with length the natural logarithm of the conditional probability that two segments 43, 44) extended into two dimensions. Sample entropy is the negative EKG time series was quantified using sample entropy estimates (32, noise to noise is the level.

Create a mapping between the signal quality measure and actual noise level. This required 613 windows for chest impedance and 882 for EKG. The noise time series was recovered using an inverse Fourier transform and normalized to unit variance.

Noise was added to the artificial time series in increasing amounts

Here \( \alpha \) is a noise-free waveform with unit variance, \( \xi \) is clinically appropriate noise time series with unit variance, and \( \sigma_{\text{noise}} \) is the fraction of variance due to noise. The time series \( Y \) has unit variance. Signal quality measures were then calculated at each value of \( \sigma_{\text{noise}} \) to create a mapping between the signal quality measure and actual noise level.

Waveform analysis: EKG noise quantification. The noise in each EKG time series was quantified using sample entropy estimates (32, 43, 44) extended into two dimensions. Sample entropy is the negative natural logarithm of the conditional probability that two segments from the time series with length \( m + 1 \) will match given that the first \( m \) points match. A match occurs when the maximum distance between two segments is less than a threshold \( r \). We choose to define matches

\[ H(y) = \frac{1}{\pi} \int_{-\infty}^{\infty} \frac{f(x)}{x - y} \, dx \]

where \( P \) indicates the Cauchy principal value of the integral. The Hilbert transform of a signal is the original signal shifted 90° in phase (41). A sample segment of six points from the time series is shown as a broken line in Fig. A1B, shifted left for clarity. Sample entropy as a function of noise level is shown in Fig. A1E for \( m = 1 \) and \( r = 0.4\sigma \), where \( \sigma \) is median absolute difference of the EKG time series.

Waveform analysis: chest impedance noise quantification. To quantify the noise in the chest impedance waveform, the power spectrum was calculated from the magnitude of a Fourier series. The power spectrum was normalized to unit area and detrended to remove the 1/f noise component. This detrending was accomplished by fitting a line to the log frequency and log power in the decade between 1 and 10 Hz, and subtracting the result from the power spectrum. The resulting spectrum consists of a peak corresponding to respiration and residual noise. By normalizing the spectrum to unit area, each ordinate corresponds to the variance at the corresponding abscissa. We therefore considered the largest ordinate to be the fraction of the time series variance corresponding to respiration. One minus the ordinate corresponds to the fraction of total variance corresponding to noise.

Fig. A2A shows a sine wave mimicking the chest impedance, and Fig. A2C shows the effect of adding 70% noise with clinically appropriate frequency content, keeping the variance equal to 1. Fig. A2, B and D, shows the corresponding normalized power spectra after

Fig. A2. A: time series of artificial chest impedance with no noise. B: normalized and detrended power spectrum for artificial chest impedance with no noise. C: time series of artificial chest impedance with 70% noise. D: normalized and detrended power spectrum for artificial chest impedance with 70% noise. E: estimated fraction of time series variance attributed to noise as a function of noise percent for a sinusoid plus clinically appropriate noise.
detrending to remove the 1/f noise component. Increasing noise distributes power across a broad frequency range and decreases the fraction of total variance due to respiration. Fig. A2E shows the mapping between the estimated fraction of time series variance due to noise and for a sinusoid plus clinically appropriate noise. The estimated fraction of time series variance due to noise saturates at low noise due to the detrending and at high noise due to residual noise in the detrended spectrum (see Fig. A2D).

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DISCLOSURES
Craig G. Rusin is CTO of Medical Informatics.

AUTHOR CONTRIBUTIONS
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